

# Probabilistic Tensor Decomposition for Human Mobility<sup>\*1</sup>

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# Introduction

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Human mobility data contains complex stochastic structure.

- **Tensor Data**

Divide the whole space into a finite number of grids and count the number of people with certain categories in each grid at specific time.

⇒ Multi-dimensional array data (= Tensor data)

- Goal: Find underlying dependence structures

⇒ Approximate the observed tensor by a parsimonious (low rank) tensor representation (= Tensor Decomposition)

We use **non-negative Tucker decomposition**.

Related literatures: Fan et al., (2014), Sun and Axhausen (2016) etc...

# Data

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We divide Tokyo metropolitan area into  $10 \times 10 = 100$  grids and count the number of people with different types of jobs at two time (00:00 and 12:00).

→ 3-dimensional tensor

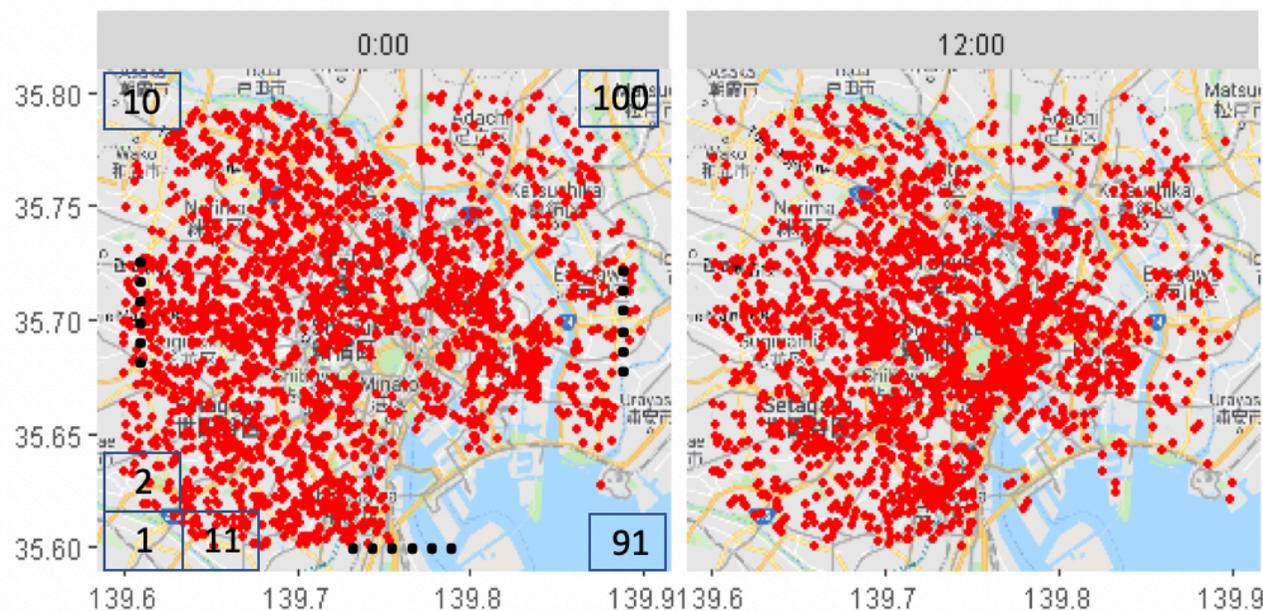


Figure1 Mobility pattern of *transportation job* at 00:00 (left) and 12:00 (right).

# Non-negative Tucker decomposition

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- $G$ : core tensor     $A, B, C$ : base matrices
- Core tensor = weight (sum of all the elements is 1)  
 $\Rightarrow$  By investigating the elements in  $A, B, C$  whose weight is large, we can see the dependence structure.

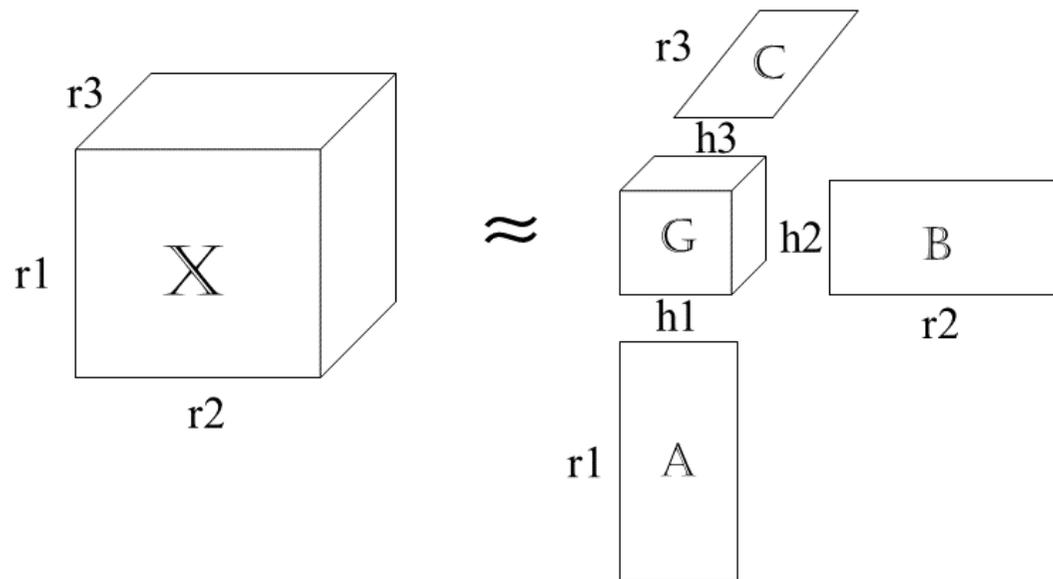


Figure2 Image of Tucker decomposition

# Non-negative Tucker decomposition

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$$x_{c_1 \dots c_m} = \sum_{k_1=1}^{h_1} \cdots \sum_{k_m=1}^{h_m} g_{k_1 \dots k_m} u_{c_1 k_1}^{(1)} \times \cdots \times u_{c_m k_m}^{(m)}$$

- $x_{c_1 \dots c_m}$ : element of observed tensor
- $g_{k_1 \dots k_m}$ : element of core tensor
- In our application,  $m = 3$  (3-dimensional tensor),  $r_1 = 100$ ,  $r_2 = 100$ ,  $r_3 = 2$  (*transportation and sales*)  
 $\Rightarrow h_1 = 16, h_2 = 16, h_3 = 2$

# Results

## Results for *transportation workers*

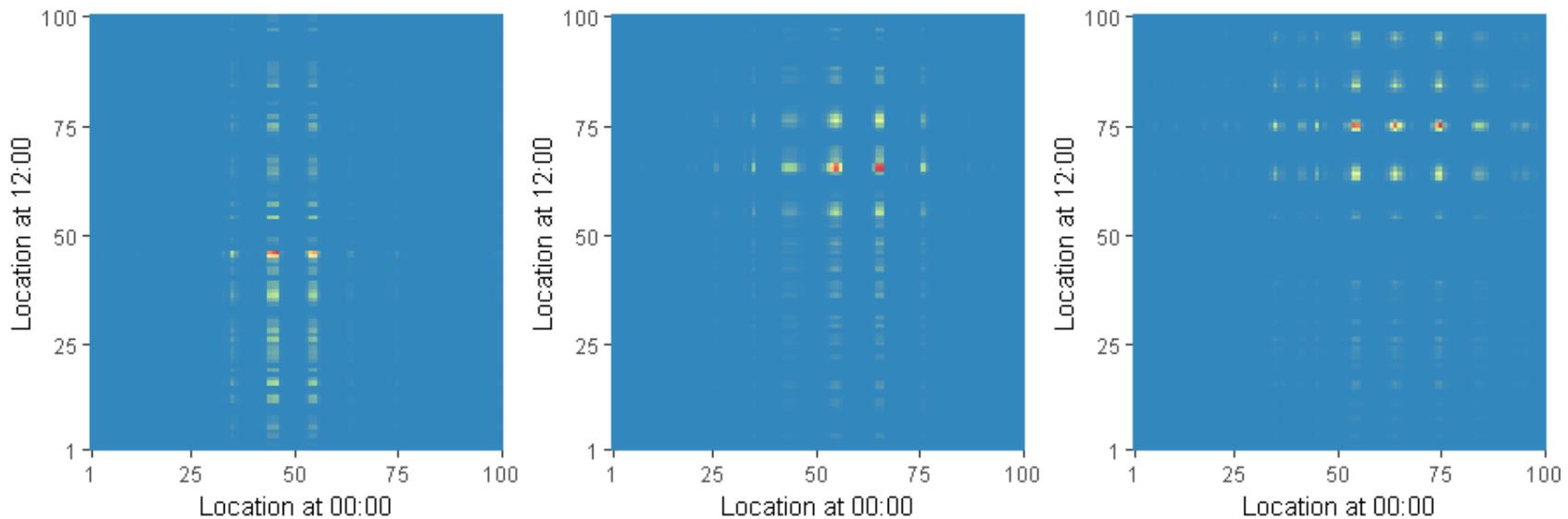


Figure3 Top 3 basis

- Base with largest weight : People are concentrated at the center of Tokyo at 00:00, but they spread at 12:00.
- Based with second and third largest weights: People remain in the east of Tokyo.

# Results

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## Results for *sales workers*

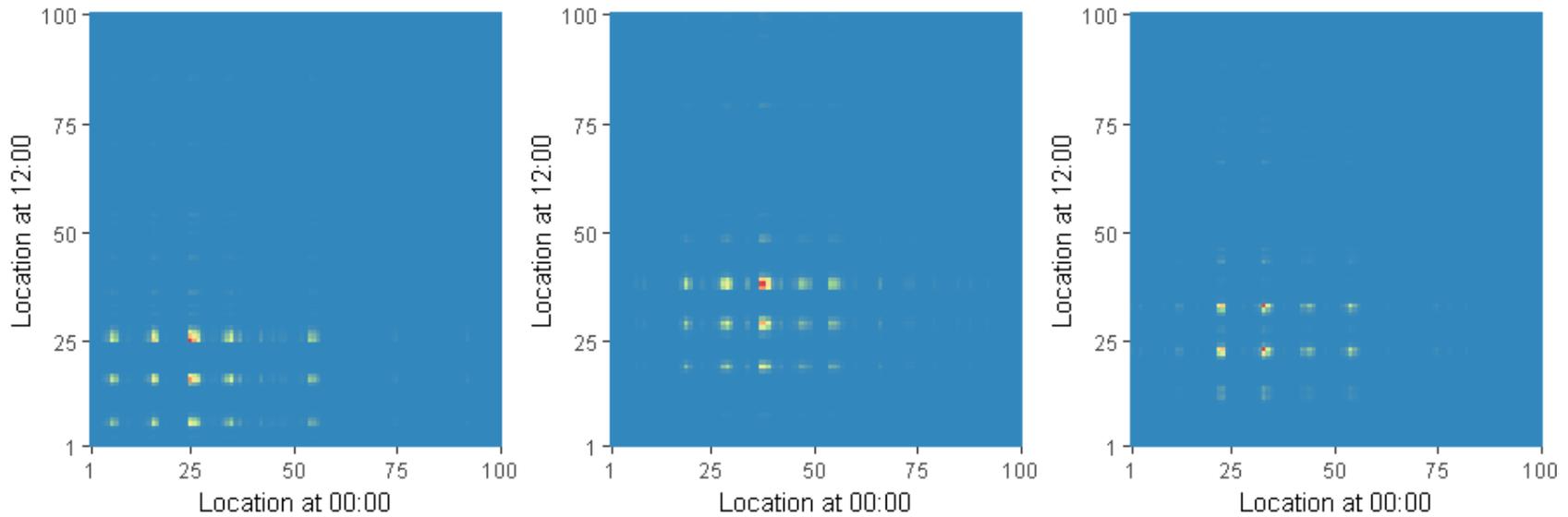


Figure4 Top 3 basis

- People are more concentrated at 12:00 than at 00:00. (Commuting?)

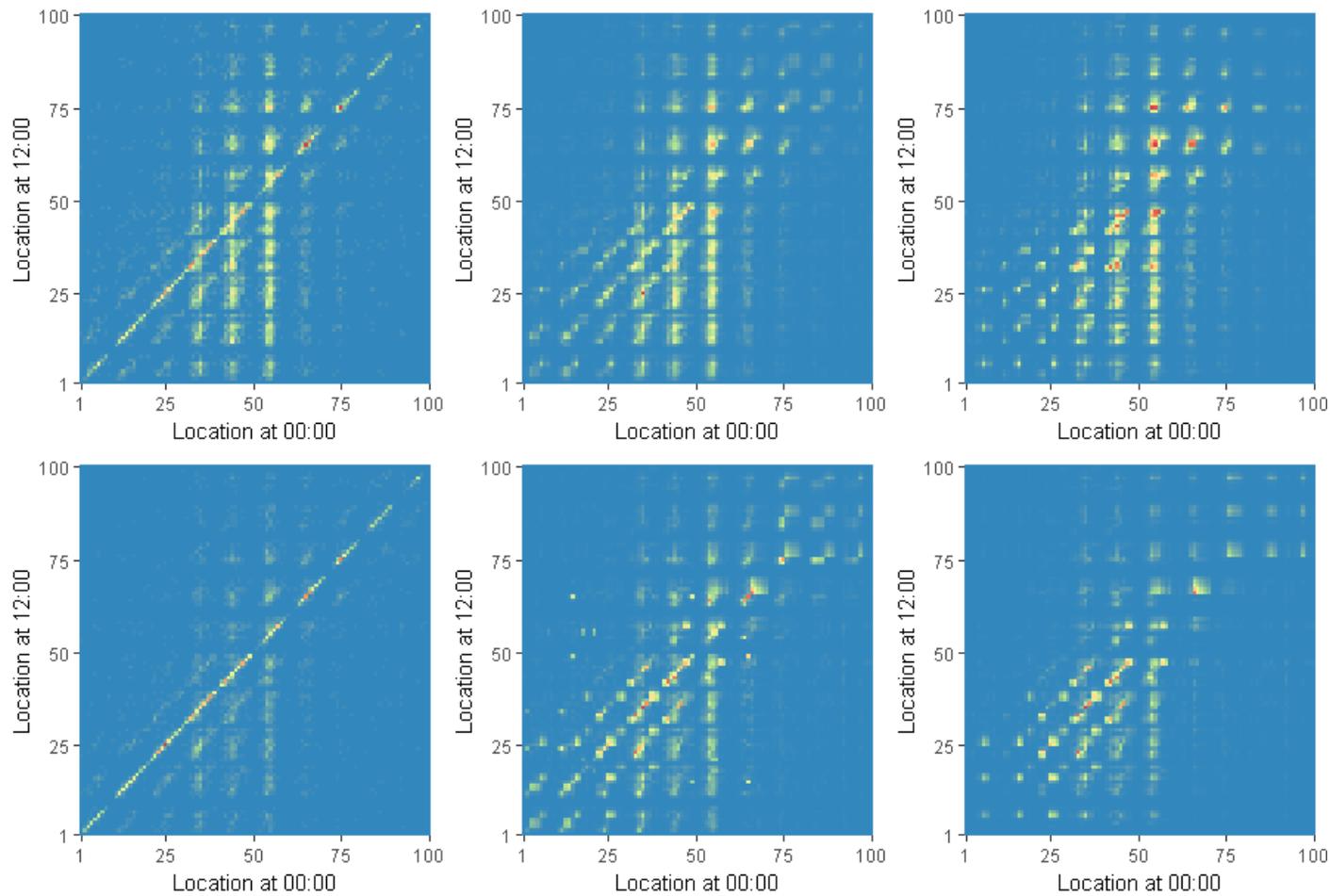


Figure5 (left) observed tensor, (center) approximated tensor, (right) approximated tensor based on bases with top 10 weights; (upper) transportation and (lower) sales workers.

# Conclusion and Future Work

- Using tensor decomposition, we can reveal the difference of human mobility among categories.

“Statistical” comparison of human mobility will be a future work.

- **Scalability**

We can use other information (Age and Purpose etc...), but the size of observed tensor will be large.

- **Clustering**

Using Dirichlet process, we may introduce clustering structure into a core tensor. (Automatic determination of the size of core tensor.)